Theories of reasoning and focal point play with a non-student sample

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Abstract
We present a coordination game experiment testing the robustness of the predictive power of level-k reasoning and team reasoning in a sample of Chinese tax administrators. We show how the incidence of coordination game play is virtually identical between Chinese tax administrators and university students, which in turn is comparable with that found in research with a Western university student sample. However, relatively to non-students, students are comparatively more attracted by the focal point under team reasoning when this has equal payoffs and the other outcomes do not.

Keywords: non-student subjects, focal points, team reasoning, level-k, coordination games.

JEL Classification: C72, C78, C91.

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1. Introduction

This paper verifies whether different theories modelling how agents play in coordination games and supported by experimental evidence with university students, generalize to a non-student sample. Specifically, we present an experiment testing the robustness of the predictive power of level-k reasoning (Stahl and Wilson, 1994; Nagel, 1995; Costa-Gomes et al., 2001) and team reasoning (Sugden, 1993; Bacharach, 1999, 2006) in a sample of Chinese tax administrators.

Traditional game theory based on the assumption of best-response reasoning cannot help individuals identify a unique solution in coordination games with more than one Nash equilibrium. However, various experimental evidence has shown that players often manage to use some salient properties of the game (i.e. cues) to converge their expectations on a unique equilibrium (i.e. the focal point); as a result, they achieve higher coordination success than what the traditional game theory predicts (Schelling, 1960; Mehta et al., 1994; Bacharach and Bernasconi, 1997; Crawford et al., 2008; Bardsley et al., 2010).

In recent years, there has been an increasing interest in theories that can explain behavior in coordination games. Team reasoning theory postulates that individuals treat themselves and their partners as a team. When dealing with coordination problems, team reasoners try to find out the best solution from the viewpoint of the team, aiming to either maximize team utility or achieve mutually beneficial outcomes. Level-k theory divides players into different cognitive levels. It assumes that the lowest level – level-0 – players make decisions non-strategically, whereas higher level players best respond to their beliefs about the behavior of the players who are one level below them. In different models of Level-k, level-0 players’ non-strategic behavior is sometimes assumed to be different. In some models, it refers to choosing randomly (Stahl and Wilson, 1994), while in others it refers to choosing the strategy that bias towards higher payoffs (Crawford et al., 2008).

Experimental evidence suggests that the predictive power of different theories is context-dependent (Bardsley et al., 2010; Faillo et al., 2017). Individuals use more team reasoning in games in which players’ interests are perfectly aligned, or in games in which the Nash equilibrium suggested by team reasoning has more equal payoffs than the payoffs in other equilibria. Individuals use more level-k in games involving conflicts of interest, or in games in which the equilibrium suggested by level-k Pareto dominates the equilibrium suggested by team reasoning. (Crawford et al., 2008; Faillo et al., 2017).

Economists have questioned whether using student subjects can lead academic experiments to generate systematically biased results. For example, Henrich et al. (2010) view student subjects as a major hindrance to generalizing results derived from experimental studies, as students are sometimes believed to be psychologically unusual and not representative to the general population. Conversely, Gächter (2010) suggests that, although the right choice of the subject pool depends on the research questions, at least in the domain of experimental economics, students are often the best subject pool, especially for
studies aiming to test theories assuming cognitive sophistication. Belot et al. (2015) contains a review of experimental evidence on student vs. non-student samples in a range of games, though not coordination games; they present the results of an experiment showing that non-students are more selfish and less rational than students from the two universities based in Oxford. They have a beauty contest game where they test level-k and find that students tend to have higher levels of reasoning, an effect that disappears once one controls for age. Bosch-Domenech et al. (2002) instead found comparable level-k results with student and non-sample samples in beauty contest games.

The debate about student subjects has started to affect focal point research. Jackson and Xing (2014) stated that they recruited subjects using Amazon Mechanical Turk because they believe university students may not be a representative subject pool for their research involving coordination/bargaining games with focal points. In spite of the concern, to date, no research has investigated the predictive power of different theories of behavior in coordination games with non-students. This paper aims to provide some evidence in this respect.

Sections 2 and 3 describe the experimental design and results, respectively. A brief discussion and conclusions are in section 4.

2. Experimental design

We employ four two-player coordination games in our experiment. In each game, subjects see a pie (see Figure 1) with three slices of equal size. We denote the three slices as S1, S2, and S3. Each slice contains two numbers separated by a comma. Each subject needs to choose a pie slice without having any communication with her partner. If she and her partner choose the same slice, they will earn a positive amount shown on that slice. From each subject’s perspective, the amount she could earn is always the number shown on the left side of the comma, and the amount her partner could earn is the number shown on the right. If the two subjects choose different slices, they earn nothing. The pie is randomly rotated across subjects, so the position of the slices could be different between a pair of subjects. This setting allows us to minimize the possibility of bringing payoff-irrelevant cues (e.g. the position of the slice) into the games.
The payoffs shown on each slice in the four games are reported in Table 1. They are variations of payoff pairs used in Faillo et al. (2017). In each game, the payoffs on S3 are always lower but more than half than those on the other two slices. Under alternative interpretations of level-k theory, this feature allows us to distinguish level-k reasoners and team reasoners. Level-k theory commonly assumes that level-0 players think non-strategically and choose whichever strategy gives them the highest material payoff without considering their partners’ behavior. In our experiment, level-k predicts that level-0 players will never choose S3, since it is strongly Pareto dominated by S1 and S2 (i.e. C, D < A, B), consequently, higher-level players who anchor their beliefs on lower-level players will never choose S3, either. Alternatively, we can reach the same conclusion if we follow Crawford et al.’s (2008) assumption that level-0 players only exist in players’ minds, in which case, even if level-0 players are assumed to play randomly, higher-level players will choose S1 or S2 rather than S3 to maximize their payoff, and S3 is never played. However, team reasoning predicts exactly the opposite. This is because, from the team’s perspective, S1 and S2 are isomorphic. In different games, the payoff pairs on these two slices are either the same or symmetric between players. Since team reasoners are unable to identify a unique solution between S1 and S2, the ex-ante expected payoffs for these two slices equal half of the payoffs shown on them. Consequently, the best strategy, from a team reasoner’s perspective, is to choose S3 since, ex-ante, its expected payoffs dominate the payoffs on the other two slices (i.e. ½ A, ½ B < C, D). Accordingly, S3 is the team-optimal slice, and (S3, S3) is the focal point.
The main difference across the four games is whether or not the payoffs are equal between players. In Game 1, payoffs are equal in S1 and S2, but unequal in S3. In Games 2 and 3, payoffs are unequal and equal in all slices, respectively. In Game 4, payoffs are unequal in S1 and S2, but equal in S3.

Table 1: Payoffs on each pie slice

<table>
<thead>
<tr>
<th></th>
<th>S1</th>
<th>S2</th>
<th>S3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Game 1</td>
<td>100, 100</td>
<td>100, 100</td>
<td>90, 80</td>
</tr>
<tr>
<td>Game 2</td>
<td>100, 90</td>
<td>90, 100</td>
<td>80, 70</td>
</tr>
<tr>
<td>Game 3</td>
<td>100, 100</td>
<td>100, 100</td>
<td>90, 90</td>
</tr>
<tr>
<td>Game 4</td>
<td>100, 90</td>
<td>90, 100</td>
<td>80, 80</td>
</tr>
</tbody>
</table>

Notes: ½ A, ½ B < C, D < A, B. Payoffs were in Chinese Yuan (RMB; 1 RMB ≅ 0.15 USD at the time of the experiment).

Experimental instructions can be found in an online appendix. We had two treatments. In the Tax-admin treatment, conducted in April 2019, subjects were tax administrators who volunteered to take part while attending a 7-day training school in Renmin university of China (n = 62). In the Student treatment, conducted in May 2019, subjects were university students at the Renmin University of China, Beijing (n = 42). The experiment was computerized by using zTree (Fischbacher, 2007). Upon arrival, subjects were randomly assigned to a terminal by drawing a tag from a bag. The experimenter read the instructions aloud. Subjects were asked to go through the instructions with the experimenter and answer a brief questionnaire to make sure that instructions were correctly understood. Subjects were not given feedback until the end of the experiment. At the end of the experiment, one game was randomly picked for each subject. Subjects’ final payments equaled their earnings of that picked game plus a 50 RMB participation fee. They had to complete a demographic questionnaire before getting paid. Sessions lasted approximately 60 minutes. The average payment was 94.33 RMB (S.D. 7.54), equivalent to approximately 14 USD at the time of the experiment.

3. Results

Figure 1 reports the proportion of times the team-optimal slice, S3, is chosen, and Table 2 shows the same data as Figure 1, plus the proportions of S1 and S2 choices. Results in both Figure 1 and Table 2 are broken down by game and treatment. In all games, except Game 4 in the Student treatment, only a small proportion of subjects chose S3. This finding is consistent with Faillo et al. (2017), who find that
team reasoning is inhibited in games in which the team-optimal equilibrium is dominated by the other two equilibria.

**Result 1:** Only a small proportion of subjects chose S3. Subjects’ behavior is more in line with level-k rather than team reasoning.

In Game 1, payoffs are equal in S1 and S2 but not in S3. Only 18% of students and 19% of tax administrators chose S3. These proportions increase to 21% and 26% respectively when payoffs in S3 also become equal (Game 3). However, the changes are not statistically significant (McNemar test p = 0.317 and p = 0.180, respectively). In Game 2, in which payoffs in all three slices are unequal, only 10% and 7% of the tax administrators and students, respectively, chose S3. These proportions increase to 24% in the Tax-admin treatment and 48% in the Student treatment when the payoffs in S3 are equal (Game 4). The differences are statistically significant (McNemar test, p = 0.003, p<0.001, respectively). The equal payoffs in the team-optimal slice can increase the choice of S3 only when the payoffs in the other two slices are unequal.

**Result 2:** The predictive power of team reasoning is facilitated if the team-optimal equilibrium gives more equal payoffs than the others.

**Figure 1:** Proportion of the team-optimal slice (S3) choices by game and treatment
Table 2: Proportion of each slice’s choices by game and treatment

<table>
<thead>
<tr>
<th></th>
<th>Tax admin (62 obs.)</th>
<th>Student (42 obs.)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>S1 (LK)</td>
<td>S2 (LK)</td>
</tr>
<tr>
<td>Game 1</td>
<td>0.48</td>
<td>0.34</td>
</tr>
<tr>
<td>Game 2</td>
<td>0.39</td>
<td>0.52</td>
</tr>
<tr>
<td>Game 3</td>
<td>0.37</td>
<td>0.42</td>
</tr>
<tr>
<td>Game 4</td>
<td>0.37</td>
<td>0.39</td>
</tr>
<tr>
<td>Average</td>
<td>0.40</td>
<td>0.42</td>
</tr>
</tbody>
</table>

In Games 1-3, tax administrators and students do not behave differently in the respect of choosing the team-optimal slice. (\(\chi^2\) test, \(p = 0.866, p = 0.652, p = 0.535\), in Games 1-3, respectively). But in Game 4, in which the team-optimal slice has equal payoffs but the other two slices do not, nearly half (48%) of the students chose S3, and this proportion is twice as many as the proportion of tax administrators choosing the same slice (24%) (\(\chi^2\) test, \(p=0.013\)). Students’ behavior is more consistent with team reasoning than tax administrators’ in a game in which only the payoffs in the team-optimal slice are equal\(^2\).

Result 3: Students and tax administrators do not behave differently in three out of four games. Students’ behavior can be better explained by team reasoning than tax administrators in a game in which the team-optimal equilibrium gives more equal payoffs than the others.

Table 3 reports the expected coordination rate (ECR) in each game. ECR is calculated as follows.

In Game 1 and Game 2, if a subject’s payoff on S3 is higher than her partner’s payoff, then we call this subject Player 1 and her partner Player 2. In Game 4, since the payoffs in S3 are the same, we define Player 1 the player whose payoff is higher in S1, and Player 2 is her partner. In each of these games, the ECR for each slice is calculated by multiplying the proportion of Player 1s who chose that slice by the proportion of Player 2s who chose that slice in that game. The total ECR is the sum of the ECR for each slice. Since payoffs in Game 3 are equal in all slices, we calculate ECR using the same way as Mehta et al. (1994) and Sitzia and Zheng (2019).

\[
ECR = \sum_i ECR_i = \sum_i \frac{n_i(n_i - 1)}{N(N - 1)}
\]

where \(N\) represents the total number of subjects, \(n_i\) represents the number of subjects who chose slice I in Game 3, and ECR\(_i\) represents the expected coordination rate for slice i,

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\(^2\) These results are replicated in regression analysis controlling for gender (see Appendix B).
The values of ECR in Tax-admin and Student treatments are nearly the same. In all games, the ECR differences across treatments are negligible (0.01-0.02). Although students chose S3 more frequently than tax administrators in Game 4, this difference does not translate into higher coordination success.

Result 4: In all games, including Game 4, the expected coordination rate in Tax-admin and Student treatments do not differ.

4. Discussion and Conclusions

In three coordination games out of four, we find the same predictive power of different models of play in coordination games with students and tax administrators. The exception is the game where the team-optimal equilibrium gives more equal payoffs than the others; in this game, students’ behavior can be better explained by team reasoning than tax administrators’. One possible reason is that equality can facilitate team reasoning more for students than tax administrators. However, in this game, like in the others, coordination rates are the same with both students and tax administrators.

Tax administrators are a highly educated professional sample, and as such, a reasonable match in socio-economic characteristics to that of university students from the good universities which normally make up the subject pool for coordination games experiments. Renmin University students are an especially good match for tax administrators since it has a long-standing tradition of producing graduates who end up in highly qualified public sector positions such as that of tax administrators. Obviously future research may wish to further stress test the robustness of our results with other, and less comparable, sample types, using coordination games with different features or frames.

While our results are with Chinese samples, they are comparable to those found in relation to the corresponding games of Faillo et al. (2017). Obviously, future research may wish to look more explicitly and systematically at cross-cultural comparisons. Taken at their face value, this finding, and our key finding of mostly robustness of the respective predictive power of team reasoning and level-k theories
with a non-student sample, speak to the potential generality of these theories and their underpinning cognitive mechanisms. However, as noted, relatively to non-students, students are comparatively more attracted by the focal point under team reasoning when this has equal payoffs and the other outcomes do not.

**References**


Appendix A: Experimental instructions (translated from Chinese)

Introduction

[oral: I will now take you through the instructions, and I will read them out.]

Welcome and thank you for taking part in this experiment. Everyone in the room has exactly the same instructions.

It is important that you remain silent and do not look at what other participants are doing. If you have any questions, or need assistance of any kind, please raise your hand and an experimenter will come to you. We expect and appreciate your cooperation.

The Pie task

At the beginning of the experiment, you will be matched with another person in the room. You and the other person will not be told each other’s identity. Your earnings will depend both on your decision and the decision of the other person.

You and the other person will need to play four Pie tasks in this experiment. An example of a Pie task is shown below.

In the pie task, you and the other person will be presented with a three-slice pie, and asked to choose one slice.

There are two amounts shown on each slice, represented by two letters. For simplicity reasons, we use the letters written on each slice to name those slices. We call the slice on the top left slice AB, on the top right slice CD, and at the bottom slice EF. **If you and the other person choose the same slice, you will earn the amount on the left of the comma of the chosen slice, and the other person will earn the amount on the right. But if you and the other person choose different slices, neither of you will earn anything in that task.**

For example, if you and the other person both choose the slice AB, you will earn amount ‘a’, and the other person will earn amount ‘b’. But if you choose the slice AB and the other person chooses slice EF, then you and the other person will earn nothing.

The orientation of the pie is randomly decided. This means that, although you and the other person will see the same pie, its orientation will vary. For example, you may see the pie shown above, while the other person may see the pie shown below.
There is no way for you to know what orientation the pie of the other person sees.

**Your earnings**

At the end of the experiment, the computer will randomly choose one of the four tasks, and your earnings in that randomly chosen task will be realised. In addition to whatever you have earned in that task, you will be given a participation fee of ¥50.

**Comprehension questionnaire**

The following questions are meant to check your understanding of the basic rules of the experiment. If anything is unclear, please raise your hand and an experimenter will come to assist you.

**Questions 1 of 4**

In the Pie task shown above, if you and the other person both chose slice CD, how much you and the other person earn in that task?

A: You earn c and the other person earns d.

B: You earn d and the other person earns c.

C: You earn a and the other person earns b.

D: You and the other person both earn nothing.

**Questions 2 of 4**

In the Pie task shown above, if you chose slice CD, and the other person chose slice AB, how much will you and the other person earn in that task?

A: You earn c and the other person earns d.

B: You earn d and the other person earns c.

C: You earn a and the other person earns b.
Questions 3 of 4

You see a pie task shown below in a pie task. What will the other person’s pie task look like?

D: All three above are possible.
Questions 4 of 4

If you are a chosen subject, your earnings of the experiment will be:

A: The sum of the earnings from all the tasks.
B: The sum of the earnings from all the tasks, plus the participation fee of ¥20.
C: The amount you earn in the randomly selected task, plus the participation fee of ¥20.
D: The amount you earn in the randomly selected task.

Correct answers:
A  D  D  C
**Appendix B: Regression results**

Model: Random effect logit (One regression for each game)

<table>
<thead>
<tr>
<th>Game</th>
<th>Treatment: Marginal effects (Standard error)</th>
<th>Gender: Marginal effects (Standard error)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Game 1</td>
<td>-0.125 (0.59)</td>
<td>0.552 (0.62)</td>
</tr>
<tr>
<td>Game 2</td>
<td>-0.790 (1.34)</td>
<td>0.773 (1.29)</td>
</tr>
<tr>
<td>Game 3</td>
<td>0.099 (0.51)</td>
<td>0.504 (0.52)</td>
</tr>
<tr>
<td>Game 4</td>
<td>0.975** (0.47)</td>
<td>0.188 (0.46)</td>
</tr>
</tbody>
</table>

n = 104 for each regression; Log likelihood = -48.97, -30.26, -55.50, and -63.29 for Game 1-4 regressions, respectively.
The dependent variable takes value 1 if the choice is S3 and 0 otherwise.

*Treatment*: dummy variable taking value 1 for Student treatment and 0 for Tax-admin treatment.

*Gender*: dummy variable taking value 0 if male and 1 if female.

*** significant at 1%; ** significant at 5%; * significant at 10%